

Inference at \* 1  
of proof for Lemma ax\_choice:

1.  $A : \text{Type}$
2.  $B : \text{Type}$
3.  $Q : A \rightarrow B \rightarrow \mathbb{P}$
4.  $\forall x:A. \exists y:B. Q(x,y)$

$\vdash \exists f:A \rightarrow B. (\forall x:A. Q(x,f(x)))$   
by ((Unfolds “all exists“ 4)  
CollapseTHEN (RenameVar ‘g’ 4)).

1:

4.  $x:A \rightarrow y:B \times Q(x,y)$

$\vdash \exists f:A \rightarrow B. (\forall x:A. Q(x,f(x)))$

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